

Разработка и реализация математической модели теплового воздействия на ограждающие конструкции, покрытые огнезащитным композитным материалом

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OpenFOAM.

Development and implementation of a mathematical model of the thermal effect on enclosing structures covered with fire-retardant composite material

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The article is devoted to the mathematical modeling of high temperature impact on the composite material when it is used as a coating for protective barriers, for example, tractor cabs for forest fire extinguishing. The composite material includes a filler, a binder water sodium glass and a hardener silicon sodium. As a filler, graphite with dimensions of several micrometers is used. The thermal effect is spatial (three-dimensional). The heat transfer at laminar motion of hot gases near the surface of the composite material, heat transfer due to radiation, as well as thermal conductivity inside the layer of composite material and the enclosure of the cabin are considered. Differential equations in partial derivatives, namely, the Navier-Stokes equations, the energy equation, the radiation transfer equation in a transparent medium, and the heat equation for solids are used to describe the processes under consideration. This system of equations is supplemented by initial and boundary conditions. The finite volume method is used for numerical analysis of the model. The calculations were carried out in a free software product OpenFOAM. As a result of the computational experiment, the fields of air temperature and the studied composite material are obtained. The mathematical model makes it possible to predict the unsteady temperature distribution in the layer of composite material and on the walls of the cabin, to calculate the time of reaching the limit state of the fire-retardant material, and also to show the dependence of the time of reaching this state on the thickness of the deposited layer.

The microcomposition provides the ability to keep unchanged the composition and structure of the thermal insulation coating under the influence of high temperatures, to maintain the bearing and enclosing functions. The results allow to evaluate the possibility of practical use of composite material for thermal protection of cabins.

Keywords: mathematical model; composite material; thermal effect; thermal protection.

« -300» « -400».

$q = q_K + q$ (1)

[18].

(dx, dy, dz) .

$\vec{F} = \vec{g}$, \vec{g} —

[1; 2].

p ,

$\mu, (\cdot) / ^2$:

[3].

$\rho, / ^3, \vec{w}; /$ —

[5],

[6],

[7].

[8],

[9–14].

$\frac{\partial t}{\partial \tau} + \nabla \cdot (wt) = a\Delta t + \frac{q_v}{\rho c_p}$, (3)

a —

c_p —

[15–17].

$q_v, \text{ / }^2,$

20°

$t, ^\circ,$

$\tau,$

$$\frac{\partial t}{\partial \tau} = a \Delta t + \frac{q_v}{\rho c_p} \quad (4)$$

20°

$$p_0 = 10^5; \quad [21]$$

$$\mu = 1,8 \cdot 10^{-5} (\cdot) / ^2;$$

$$c_p = 1$$

$$/ (\cdot);$$

$$c_p = 1,2 / (\cdot);$$

$$\rho = 1172 / ^3;$$

$$\lambda = 1, / (\cdot) [15].$$

$$20 [17].$$

$$\nabla \cdot \vec{w} = 0.$$

(1)–(5)

[1; 18].

$$(1)–(5) \quad q_v = 0.$$

(1)–(5)

$$\vec{w} = 0.$$

$$(\cdot 1)$$

$$\vec{w} = (0; 0; 1; 0).$$

$$\frac{\partial \vec{w}}{\partial y} = 0.$$

[19; 20].

. 1.

()

. 2.

(1)–(5).

$$\frac{\partial p}{\partial x} = 0; \quad \frac{\partial p}{\partial y} = 0; \quad \frac{\partial p}{\partial z} = 0$$

$$p_y = p_0.$$

[20]:

$$t - t_0 = 345 \cdot \lg(8 \cdot \tau + 1), \quad (6)$$

$t, ^\circ$

$\tau; t_0, ^\circ$

20°

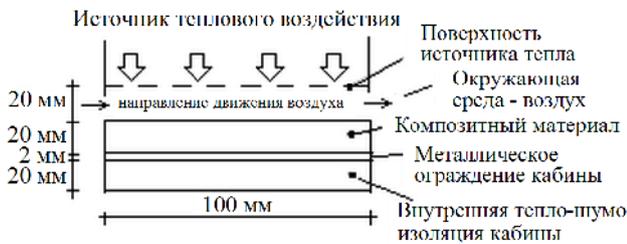
$$\frac{\partial t}{\partial n} = 0, \quad n$$

III

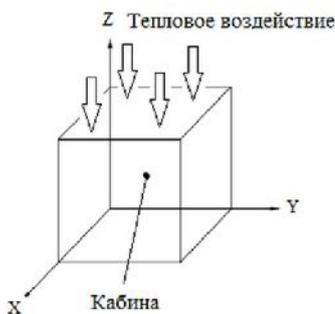
(1)–(5)

[1].

$$h_x = 10, \quad h_y = 10, \quad h_z = 2.$$



. 1.



. 2.

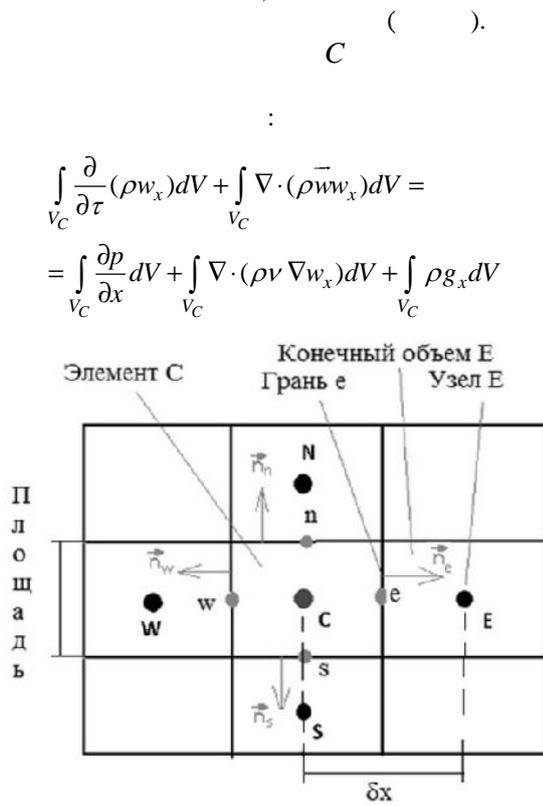
$$[20] \quad \vec{w}_0 = (0; 0; 1; 0).$$

0 / .

3. (5)

$$\int_{V_C} \nabla \cdot (\rho \bar{w} w_x) dV = \int_{\partial V_C} (\rho \bar{w} w_x \cdot \bar{n}_f) dS = \sum_{f \in nb} \rho \cdot \bar{w} \cdot S_f \cdot \bar{n}_f \cdot \left(\frac{\partial w_x}{\partial x}; \frac{\partial w_x}{\partial y}; \frac{\partial w_x}{\partial z} \right)_f$$

$$\int_{V_C} \nabla \cdot (\rho \bar{w} w_x) dV = \int_{\partial V_C} (\rho \bar{w} w_x \cdot \bar{n}_f) dS = \sum_{f \in nb} \rho \cdot \bar{w} \cdot S_f \cdot \bar{n}_f \cdot \left(\frac{\partial w_x}{\partial x}; \frac{\partial w_x}{\partial y}; \frac{\partial w_x}{\partial z} \right)_f$$



3.

$$\int_{V_C} \frac{\partial}{\partial \tau} (\rho w_x) dV = \frac{w_x^c(\tau_i) - w_x^c(\tau_{i-1})}{\Delta \tau} \cdot \rho \cdot V_C$$

$\Delta \tau = \tau_i - \tau_{i-1} = 0,005$, i :

$$\int_{V_C} \nabla \cdot (\rho \bar{w} w_x) dV = \int_{\partial V_C} (\rho \bar{w} w_x \cdot \bar{n}) dS = \sum_{f \in nb} \rho \cdot \bar{w} \cdot S_f \cdot \bar{n}_f \cdot w_x^f = \sum_{f \in nb} \dot{m}_f \cdot w_x^f$$

∂V_C — C ; nb — $f = 1 \dots 6$ — nb ; S_f — f ; \bar{n}_f — f ; \dot{m}_f — f :

$$\int_{V_C} \frac{\partial p}{\partial x} dV = - \left(\frac{\partial p}{\partial x} \right) \cdot V_C$$

$$\int_{V_C} \rho g_x dV = 0$$

$$\int_{V_C} \nabla \cdot (\rho \bar{w}) dV = 0$$

$$\int_{V_C} \nabla \cdot (\rho \bar{w}) dV = \int_{\partial V_C} (\rho \bar{w} \cdot \bar{n}) dS = \sum_{f \in nb} \rho \cdot \bar{w} \cdot S_f \cdot \bar{n}_f = \sum_{f \in nb} \dot{m}_f$$

$$\sum_{f \in nb} \dot{m}_f = 0$$

$$\int_{V_C} \frac{\partial}{\partial \tau} (\rho H) dV + \int_{V_C} \nabla \cdot (\rho \bar{w} H) dV = \int_{V_C} \nabla \cdot (\alpha \nabla H) dV$$

$$\int_{V_C} \frac{\partial}{\partial \tau} (\rho H) dV = \frac{H^C(\tau_i) - H^C(\tau_{i-1})}{\Delta \tau} \cdot \rho \cdot V_C$$

$$\int_{V_C} \nabla \cdot (\rho \bar{w} H) dV = \int_{\partial V_C} (\rho \bar{w} H \cdot \bar{n}) dS = \sum_{f \in nb} \rho \cdot \bar{w}_f \cdot n_f \cdot S_f \cdot H^f = \sum_{f \in nb} \dot{m}_f \cdot H_f$$

$$\int_{V_C} \nabla \cdot (\alpha \nabla H) dV = \int_{\partial V_C} (\alpha \nabla H \cdot \bar{n}) dS = \sum_{f \in nb} \alpha \cdot S_f \cdot \bar{n}_f \cdot \left(\frac{\partial H}{\partial x}; \frac{\partial H}{\partial y}; \frac{\partial H}{\partial z} \right)_f$$

$$\int_{V_C} \frac{\partial}{\partial \tau} (\rho H) dV = \int_{V_C} \nabla \cdot (\alpha \nabla H) dV$$

$T_1,$

$e_2 = 0,289,$

$\frac{\partial I}{\partial n} = 0,$

C (.3)

$\int_{V_c} \nabla \cdot (\vec{d}_{AVE} I) dV = 0 .$

$\int_{V_c} \nabla \cdot (\vec{d}_{AVE} I) dV = \int_{\partial V_c} (\vec{d}_{AVE} I \cdot \vec{n}) dS$
 $= \sum_{n \in nb} \vec{d}_{AVE} \cdot S_n \cdot \vec{n}_n \cdot I_n = 0$

$\nabla \cdot (\vec{d}_{AVE} I) = 0$

$d_{AVEx} \frac{\partial I}{\partial x} + d_{AVEy} \frac{\partial I}{\partial y} + d_{AVEz} \frac{\partial I}{\partial z} = 0 ,$ (7)

$I,$; d_{AVE}

(1)-(7).

« » « » (.1):

« »:

« »;

« »: « - -

»

« », -

$I = \frac{1}{\pi} \cdot e_1 \cdot \sigma \cdot T^4 .$ π

[20].

; $e_1 = 1,$

; $\sigma = 5,67,$ // ($^2 \cdot ^4$) -

; $T,$ - (

(6).

$220^\circ,$

$\frac{\partial I}{\partial n} = 0,$ n

(.4).

« - 1- : . b - , . c -

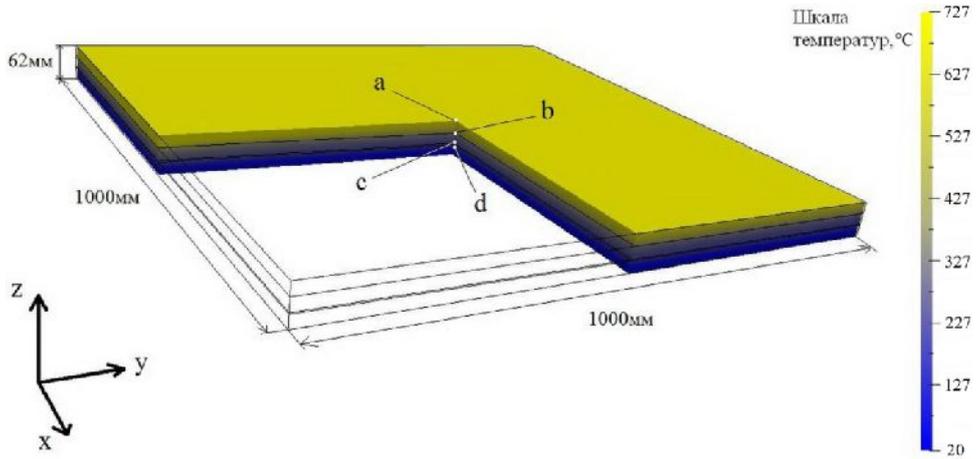
$I_k = \frac{1}{\pi} \cdot ((1-e_2) \cdot I_{\tau-1} + e_2 \cdot \sigma \cdot T_1^4),$

$\Delta\tau = \tau_i - \tau_{i-1} = 0,005,$ -

$i.$ ($1-e_2$) $\cdot I_{\tau-1}$

900 [20].

$e_2 \cdot \sigma \cdot T_1^4$



. 4.

(6),
738 ° .

, 900 ,

391 ° .

391 °

[17].

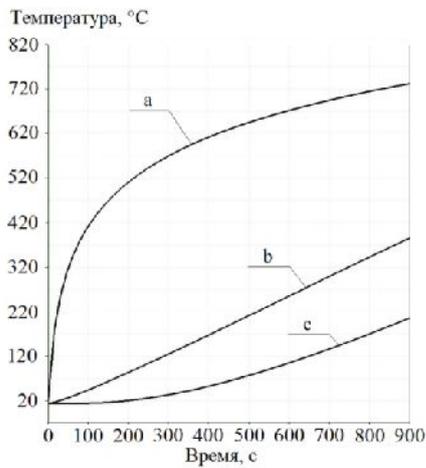
930
20 ,

[20].

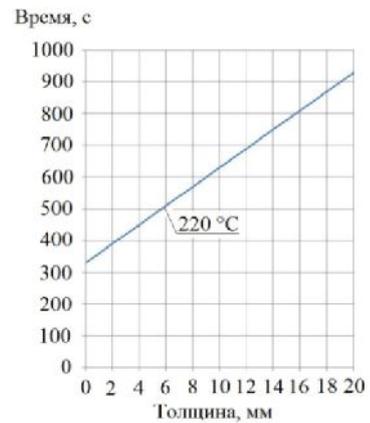
[17]

900 ° .
«

» 211 ° .



. 6.



220 °

. 5.

: a —
; b —

« —

» ; —

« —

»

,

. 7

287 °

, 900 ,
220 ° .

[21],
20

1 104 .

381 .

(. 6).

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